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A NEW ALGORITHM FOR TIME SERIES DATA MINING BY USING ROUGH SET

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Abstract: This paper is to apply Rough Set to data mining of time series. Firstly, we process the time series data by attribute selection and similarity sequence search. Secondly, the time series is partitioned into some sets of pattern by Mobile Window Method (MWM) and each pattern is a trend of time series. Thirdly, an information table is made by predicting attributes and targeting attribute in trending variation ratio structure sequence (TVRSS). Then, the original information table is made suitably for rough set to discover knowledge. Finally, the extracting rules can predict the time series behavior in the future. The total process is four steps. In the end, we show some examples to demonstrate our method on the time series data of stock market.

Keywords: TVRSS, Time series, Rough Set, Prediction.

1. INTRODUCTION

Time-series data is becoming more and more vital in much field, especially in economic and finance area. With broad application of the information technology and diversification approach of obtaining data, time series information is increasing rapidly. People often try to mine the potential knowledge and useful information in some effective method or technologies when they confront a great deal of time series data. For example, consumers often make use of historical stock closing price data to predict future closing price. The procedure of converting historical data to useful knowledge or information for human is paid more attention in modern society.

Time-series data mining is an important way which mining some useful and potential knowledge from a great deal of time-series [1]. More and more people began to pay more attention to time-series data mining [2, 3, 4]. Nowadays, the study about time-series mining is mainly about similarity mining and time sequences query. Due to nonlinear, aperiodic and chaos of time series, it is difficult to predict future precision for human. But in a certain situation, it is possible to predict some potential information in time-series. For example, if you have necessary information about trend of stock closing price. We can predict the approximately trend in the future in spite of we can't predict the precise closing price.

In this paper, we mainly discussed the time-series data prediction based on TVRSS and rough set. Section 2 is devoted to introducing time-series and trending variation ratio structure sequence. Section 3 deals with some basic notions related to rough set theory (RST). In section 4, a novel time-series prediction method based on TVRSS and a timeseries data mining model based on rough set are proposed respectively. Section 5 is experimental analysis. Conclusion is section 6.

2. TIME SERIES AND TVRSS

Time series is a series of observation data according to a certain time sequence [5]. It is a aggregate which has time and event. Time series is a data set in the planar or multidimensional space. Time-series data mining is a important way which mining some useful and potential knowledge from a great deal of time-series [6].

Time series possess characteristic as follows:

1. In a planar time series X, a certain point x_t is composed of abscissa time T and y-axis X (t, x) in planar space T \times X.

2. Time series is not reversible.

3. Information transfer is unilateral and not reversible; Information transfer direction is same as

the time. For example, a time series $X=\{x_t|t=1, 2, ..., n\}$. Information will transfer with x_{t1} to x_{t2} ($t_1 < t_2$).

Definition 1 [5] For a planar time series $X = \{x_t | t=1, 2, ..., n\}$, a certain point x_t is composed of abscissa time T and y-axis X (t, x) in planar space T $\times X$. We can write time series in vector form

$$X = \{x_1, x_2, ..., x_n\}$$

Definition 2 Let $X = \{x_t | t=1, 2,...,n\}$ be time series, $\lambda = \{\lambda_1, \lambda_2,..., \lambda_{n-1}\}$. λ is a trending variation ratio structure sequence of X. In which, $\lambda i = \lambda i = \frac{\Delta i_x}{\Delta i_T}$, $\Delta i_x = x_{i+1} - x_i$, $\Delta i_t = t_{i+1} - t_i$ Obviously,

 λ is also a time series.

$$\lambda = \left\{ \frac{\Delta \quad 1}{\Delta \quad 1}, \frac{\Delta \quad 2}{\Delta \quad 2}, \dots, \frac{\Delta \quad n-1}{\Delta \quad n-1} \\ \frac{\Delta \quad 1}{\Delta \quad 1}, \frac{\Delta \quad 2}{\Delta \quad 1}, \dots, \frac{\Delta \quad n-1}{\Delta \quad n-1} \right\}$$
(1)

in which, $I = \{1, 2, ..., n-1\}$.

Definition 3 Let $X = \{x_t | t=1, 2, ..., n\}$ be time series, $\lambda = \{\lambda_1, \lambda_2, ..., \lambda_{n-1}\}$ be trending variation ratio structure sequence of X. $(x_i, x_{i+1},..., x_{i+k-1})$, $(\lambda_j, \lambda_{j+1},..., \lambda_{j+k+1})$ (I=1, 2, ..., n-k+1; j=1, 2, ..., n-k) are called k=time sub series for X and λ respectively. $\{\lambda_h, \lambda_{h+1},..., \lambda_{h+k-1}\}$ is a trending variation ratio structure sequence of time sub series $\{x_h, x_{h+1}, ..., x_{h+k-1}\}$ in λ . In which, $\lambda_m = \frac{\Delta m}{\Delta T}$, m=h, h+I,..., h+k-1 (h+k-1<p) xi \in Y: $\{x_1, x_2, ..., x_{n-k}\}$ is a latest time

(h+k-1<n), $xi \in X$; { $x_h, x_{h+1}, ..., x_{h+k-1}$ } is a latest time sub series which length is k of X.

k-time sub series is defined as follows,

$$S(X, k) = \{(x_i, x_{i+1}, \dots, x_{i+k-1}) | (i=1, \dots, n-k+1)\}$$
(2)

$$S(\lambda, k) = \{ (\lambda_{j}, \lambda_{j+1}, ..., \lambda_{j+k-1}) | (j=1, 2, ..., n-k) \}$$
(3)

Here, |S(X, k)|=n-k+1, $S(\lambda, k)=n-k$.

Definition 4 Suppose s_1 , $s_2 \in S(X, k)$ -{ $(x_{n-k+1}, x_{n-k+2}, ..., x_n)$ }, ι_1 , $\iota_2 \in S(\lambda, k)$, ι_1, ι_2 are trending variation ratio structure sequence of s_1, s_2 respectively. If $d(\iota_1, \iota_2)=0$, then the trending variation ratio structure of s_1 is same as s_2 . In which, $d(\iota_1, \iota_2)$ denotes the Euclid distance, $d(\iota_1, \iota_2) = \sum_{i=1}^{k} |\lambda_{1i} - \lambda_{2i}|$, $\iota_1 = \{\lambda_{11}, \lambda_{12}, ..., \lambda_{1k}\}$, $\iota_2 = \{\lambda_{21}, \lambda_{22}, ..., \lambda_{2k}\}$.

Definition 5 Suppose $X = \{x_t | t=1, 2, ..., n\}$ be time series, $\triangle_{x}^i = x_{i+1} - x_i, \triangle_{T}^i = t_{i+1} - t_i, i=1, 2, ..., n-1,$ $\lambda = \left\{ \frac{\triangle_{x}^1}{\triangle_{T}^1}, \frac{\triangle_{x}^2}{\triangle_{T}^2}, ..., \frac{\triangle_{x}^{n-1}}{\triangle_{T}^{n-1}} \right\}$ is the trending variation ratio

structure sequence of X, then the trending variation ratio structure sequence of X are redefined as follows according to various $\frac{\Delta i}{\Delta i}_{T}^{i}$,

$$\lambda^{k} = \begin{cases} \left\{ \begin{cases} \frac{\Delta}{n} \frac{i}{x} & | \frac{\Delta}{n} \frac{i}{x} > 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} > 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} = 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} = 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} < 0 \\ \frac{\Delta}{n} \frac{i}{T} & | \frac{\Delta}{n} \frac{i}{T} & \frac{\Delta}{n} \frac{i}{T} \\ \frac{\Delta}{n} \frac{i}{T} & \frac{\Delta}{n} \frac{i}{T} & \frac{\Delta}{n} \\ \frac{\Delta}{n} \frac{i}{T} & \frac{\Delta}{n} \frac{i}{T} & \frac{\Delta}{n} \\ \frac{\Delta}{n} & \frac{i}{T} & \frac{\Delta}{n} \\ \frac{\Delta}{n} & \frac{i}{T} & \frac{i}{T} & \frac{\Delta}{n} \\ \frac{\Delta}{n} & \frac{i}{T} \\ \frac{i}{T} & \frac{i}{T} &$$

in which, $\triangle_{T}^{i} > 0$ corresponding to ascending trending structure sequence λ^{1} . $\triangle_{T}^{i} = 0$ corresponding to ascending trending structure sequence λ^{2} . $\triangle_{T}^{i} < 0$ corresponding to ascending trending trending trending trending trending structure sequence λ^{3} .

3. DECISION-MAKING INFORMATION SYSTEM IN ROUGH SET THEORY

Information is a cognitive result about external world and a decision-making principle about human behavior. People can make some useful decisionmaking by historical knowledge, especially in prediction field and reasoning technology. Information system is a abstract description of database. Data in information system is usually denoted by relation table which row denotes objects and column denotes attributes. Information of objects is expressed by attribute value. It is an important tache between objects and attribute. It is also an information foundation for knowledge discovery.

Definition 6 [8] Let U be a non-empty, finite set of objects called the universe, R be an equivalence relation on U. The pair (U, R) as approximation space. And a set of equivalent classes with respect to R is as follows

$$U/R = \{ [x_i]_R | x_i \in U \},\$$

and where $[x_i] = \{x_j | (x_i, x_j) \in R\}$.

Definition 7 [8] Information System (IS) is a quaternary presentation

$$S=(U, A, V, f)$$

in which, U denotes a non-empty, finite set of objects called the universe, it is expressed as $U=\{x_1, x_2, ..., x_n\}$. A denotes a noe-empty, finite set of attribute it is expressed as $A=\{a_1, a_2, ..., a_m\}$. V is range of attribute. $V=\{v_1, 2, ..., v_m\}$ where v_i is a value of a_i . f is a information function, f: $U \times A \rightarrow V$, $f(x_i, a_i) \in V_i$

Definition 8 [8] Decision Information System (DIS) is a quaternary presentation

S=(U, CUD, V, f)

where $A=C \cup D$ and $C \cap D \neq 0$ in which, C is the set of conditional attribute and D is the set of decision attribute.

Definition 9 [8] Each non-empty subset $p \subseteq A$ determines an indiscernibility relation as follows:

 $IND(p) = \{(x, y) \in U \times U | f_i(x) = f_i(y), a_i \in p\},\$

then IND(p) is an equivalence relation on U and let:

 $[x_i]_{\text{IND}(p)} = \{x_j | (x_i, x_j) \in \text{IND}(p)\}.$

Property 1 IND(p) is an equivalence relation on U and IND(p)= $I_{a\in p}$ IND(a)

Definition 10 Let $S=\{U, A, V, f\}$ be a decisionmaking information system, where $A=C \cup D$ and $C \cap D \neq 0$ $X_i=U/C$, $Y_j=U/D$ Decision-making rules are defined as follows:

$$\mathbf{r}_{ij} : \operatorname{des}(X_i) \rightarrow \operatorname{des}(Y_j) \quad X_i \cap Y_j \neq 0$$
(5)

in which $des(X_i)$ denotes the description of each object on conditional attributes, and $des(Y_j)$ denotes the description of each object on decision-making attribute.

Corollary 1 Reliability gene of each rule is defined as follows,

$$\mu(X_i, Y_j) = |X_i \cap Y_j| / |X_i|$$

where, $0 \le \mu(X_i, Y_j)$

if
$$\mu(Xi, Yj) = 1$$
, then r_{ii} is certain;

if $0 \le \mu(Xi, Yj) \le 1$, then r_{ij} is uncertain

Example 1 Give a decision-making table of insurance investigation in TaiWan (see Table 1), in which U={person1, person2,..., person8}={x1, x2,..., x8}, A={area, occupation, age, salary, insurance}={a1, a2, a3, a4, a5},

C={area, occupation, age, salary}={a1, a_2 , a_3 , a_4 },

 $D = \{insurance\} = \{a_5\}$

In above insurance investigation, conditional attributes and decision attribute are described as follows,

area={north, south}={1, 2};

Age={young, middleage, old}= $\{1, 2, 3\};$

Salary= $\{low, high\} = \{1, 2\};$

Insurance={living, poverty, house}= $\{1, 2, 3\};$

Xi=U/C={{x1, x3}, {x2}, {x4, x5, x7}, {x6, x8}} Yi=U/D={{x1, x2, x3}, {x4, x5, x7}, {x6, x8}}

For example, according to Eq. (4), we can obtain some useful decision-making rules easily:

Table 1. Insurance investigation

person	area	occupation	age	salary	insurance
x ₁	1	1	3	2	1
x ₂	2	1	2	1	1
X ₃	1	1	3	2	1
x4	1	2	2	1	2
X ₅	1	2	2	1	2
x ₆	1	2	1	1	3
X ₇	1	2	2	1	2
X ₈	1	2	1	1	3

Rule 1 If a person who lived in north of Taiwan, is a old worker, and have high salary, then he or she will buy living insurance;

Rule 2 If a person who lived in south of Taiwan and is middle age worker, **and** have low salary, then he or she will buy living insurance;

Rule 3 If a person who lived in north of Taiwan and is old worker, and have low salary, then he or she will buy living insurance;

Rule 4 If a person who lived in north of Taiwan and is middle age professor, and have high salary, then he or she will buy poverty insurance;

According to corollary 1, above rules are certain, because of their $\mu(X_i, Y_i)=1$.

4. TIME-SERIES DATA PREDICTION BASED ON TVRSS AND ROUGH SET

After introduced the basic concept of time series and decision-making information system in rough set theory. In this section, a model of time-series data mining based on rough set is established firstly, then a novel time-series data prediction method based on trending variation ratio structure sequence and rough set is proposed.

4.1. TIME-SERIES DATA MINING MODEL BASED ON ROUGH SET

Generally, data mining procedure is divided into steps as follows,

1. Establish data mining goal

2. Analysis and prepare data

3. Establish mining model according correlative algorithm

4. Evaluate mining model

5. Implement data mining

Without exception, time-series data mining model based on rough set contains data collection, data pretreatment, data reduction, extracting rules, classification and prediction [11].

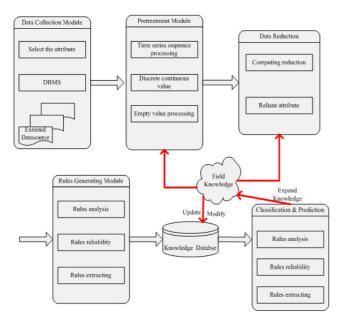


Fig. 1 – Time-series data mining model based on rough set

4.2. CONVERSION FROM TVRSS TO DECISION IN-FORMATION SYSTEM

Suppose time series $X = \{x_1, x_2, ..., x_n\}$, trending variation ratio structure sequence $\lambda = \{\lambda_1, \lambda_2, ..., \lambda_{n-1}\}$ Conversion step as follows:

- **step 1** Data standard pretreatment for λ by mobile window method [9].
- **step 2** Make trending variation ratio structure sequence convert into standard time-series data stylebook set.
- **step 3** Make standard time-series data stylebook set convert into decision-making information system.

Suppose mobile window size=k, we can construct trending variation ratio structure information system according to above steps, (see Table 2). Here, trending variation ratio structure information system reflects feature sub sequence property. So, we can analyze the time-series data with feature sub sequence.

Table 2. TVRSS information system

U∖A	a_1	a ₂	 a _{k-2}	a _{k-1}	a_k
1	$a_1 \lambda_1$	λ_2	 $\lambda_{ ext{k-2}}$	$\lambda_{ ext{k-1}}$	$\lambda_{ m k}$
2	λ_2	λ_3	 $\lambda_{ ext{k-1}}$	λ_k	λ_{k+1}
3	λ_3	λ_4	 $\lambda_{ m k}$	λ_{k+1}	λ_{k+2}
4	$egin{array}{c} \lambda_2 \ \lambda_3 \ \lambda_4 \end{array}$	λ_{5}	 λ_{k+1}	λ_{k+2}	λ_{k+3}
n-k	$\lambda_{ m n-k}$	$\lambda_{\rm n-}$	λ_{n-3}		
	· 11=K	k+1	 · II=3	- 11=2	- 11-1

Table 3. TVRSS predictable information system

U\A	a_1	a ₂	 a _{k-2}	a _{k-1}	a_k
1	λ_{1}	λ_2	 $\lambda_{ ext{k-2}}$	λ_{k-1}	λ_k
2	λ_2	λ_3	 $\lambda_{ ext{k-1}}$	$\lambda_{ m k}$	λ_{k+1}
3	λ_3	λ_4	 $\lambda_{ m k}$	λ_{k+1}	λ_{k+2}
4	λ_4	λ_{5}	 λ_{k+1}	λ_{k+2}	λ_{k+3}
n-k	λ_{n-k}	λ _{n-} _{k+1}	 λ_{n-3}	λ_{n-2}	λ_{n-1}
s _q	λ _{n-} _{k+1}	λ_{n-k+2}	 $\lambda_{\text{n-2}}$	λ _{n-1}	q

4.3. ONE-STEP PREDICTION BASED ON TVRSS PREDICTABLE INFORMATION SYSTEM

In time series $X=\{x_1,x_2,...,x_n\}$, One-step prediction is that predict X_{n+1} value. But, it can't predict precise value, only predict the trend on time n+1. Time-series trending variation ratio structure in latest mobile window is $\{\lambda_{n-k+1}, \lambda_{n-k+2},...,\lambda_{n-1}\}$, decision attribute value q is unknown, decision attribute value q is the prediction aim(q=-1,0,1) (see Table 3).

In Table3, different trending variation ratio depicts different pattern. These values are continuous, it is necessary to discrete these values according to its variation ratio. Here, fuzzy discrete method is adopted.

4.3.1 DATA PRETREATMENT

Definition 11 Suppose $X = \{x_t | t=1,2,...,n\}$ be time series, the trending variation ratio structure $\lambda = (\frac{\Delta}{X} \frac{1}{T}, \frac{\Delta}{X} \frac{2}{T}, ..., \frac{\Delta}{X} \frac{n^{-1}}{T}),$ the membership function of transform variation ratio on $\lambda = 1$.

functions of trending variation ratio on, $\lambda_1, \lambda_2, \lambda_3$ are defined respectively as follows,

$$\begin{split} \mu_{ascend_{rapid}} &= \begin{cases} 0, & |\lambda_{i}| \leq b_{1} \\ \frac{|\lambda_{i}| - |b_{1}|}{a_{1} - b_{1}}, & b_{1} \leq |\lambda_{i}| \leq a_{1} \\ 1, & |\lambda_{i}| \geq a_{1} \end{cases} \\ \mu_{ascend_{moderate}} &= \begin{cases} 0, & |\lambda_{i}| \leq b_{2} \\ \frac{|\lambda_{i}| - |b_{2}|}{a_{2} - b_{2}}, & b_{2} \leq |\lambda_{i}| \leq a_{2} \\ 1, & |\lambda_{i}| \geq a_{1} \end{cases} \\ \mu_{ascend_{slow}} &= \begin{cases} 0, & |\lambda_{i}| \leq b_{3} \\ \frac{|\lambda_{i}| - |b_{3}|}{a_{3} - b_{3}}, & b_{3} \leq |\lambda_{i}| \leq a_{3} \\ 1, & |\lambda_{i}| \geq a_{1} \end{cases} \end{split}$$
(6)

In Eq. (6), $\lambda_i \in \lambda^1$

$$\mu_{equal} = 1 \quad \mathbf{c} \leq |\lambda_i| \leq d \quad (7)$$

Here, $\lambda_i \in \lambda^2$

$$\begin{split} \mu_{descend_{rapid}} &= \begin{cases} 0, & |\lambda_{i}| \leq f_{1} \\ \frac{|\lambda_{i}| - |f_{1}|}{e_{1} - f_{1}}, & f_{1} \leq |\lambda_{i}| \leq e_{1} \\ 1, & |\lambda_{i}| \geq e_{1} \end{cases} \\ \mu_{descend_{mod\,erate}} &= \begin{cases} 0, & |\lambda_{i}| \leq f_{2} \\ \frac{|\lambda_{i}| - |f_{2}|}{e_{2} - f_{2}}, & f_{2} \leq |\lambda_{i}| \leq e_{2} \\ 1, & |\lambda_{i}| \geq e_{2} \end{cases} \\ \mu_{descend_{slow}} &= \begin{cases} 0, & |\lambda_{i}| \leq f_{3} \\ \frac{|\lambda_{i}| - |f_{3}|}{e_{3} - f_{3}}, & f_{3} \leq |\lambda_{i}| \leq e_{3} \\ 1, & |\lambda_{i}| \geq e_{3} \end{cases} \end{cases}$$
(8)

In Eq. (8), $\lambda_i \in \lambda^3$

In which, $a_1,a_2,a_3,b_1,b_2,b_3,c,d,e_1,e_2,e_3,f_1,f_2,f_3$ is defined by users

The trending variation ratio structure sequence $\Pi = \left\{ \frac{\Delta}{1} \frac{1}{X}, \frac{\Delta}{2} \frac{2}{T}, \dots, \frac{\Delta}{2} \frac{n^{-1}}{T} \right\} \text{ is redefined according to}$

above membership functions of trending variation radio as follows,

$$\tilde{\lambda} = (\mu_1^1, \mu_2^1, \dots, \mu_7^1, \dots, \mu_1^{n-1}, \mu_2^{n-1}, \dots, \mu_7^{n-1})$$
(9)

Moreover, Eq. (9) is formalized according to the maximum membership grade principle like this,

e.g.
$$\hat{\lambda} = (0, 1, 0, 0, 0, 0, 0 | 0, 0, 0, 0, 1, 0, 0 | 0, 0, 0, 1, 0, 0, 0 | 1, 0, 0, 0, 0, 0, 0)$$
 (10)

Eq. (10) depicts the feature of trending on variation ratio. So, its feature is explained as follows,

$$ascend_{mod\,erate} \rightarrow descend_{rapid} \rightarrow equal \rightarrow ascend_{rapid}$$

Obviously, redefined $\tilde{\lambda}$ is constituted by sevendimensional vector space. However, we can get the trend of future time according to the $\tilde{\lambda}$ corresponding to its state space vector.

4.3.2 PATTERN MATCHING

In this paper, we consider each trending structure sequence is a pattern.Due to this idea, Hamming distance is adopted in this paper.

Definition 12 Suppose a certain pattern $l_{n-k} = (\lambda_{n-k}, \lambda_{n-k+1}, ..., \lambda_{n-1}) \in S(\lambda, k)$, the trending structure state space vector of l_{n-k} is denoted as follows,

$$\tilde{\lambda}^{n-k} = (p_{n-k1}, p_{n-k2}, ..., p_{n-kn-k+1})$$

k=1,2...,n-k+1 (11)

Definition 13 Let

 $s_1, s_2 \in S(X, k) - \{(x_{n-k+1}, ..., x_n)\}, l_1, l_2, \in S(\lambda, k), l_1, l_2$ are the time sub series of s_1m, s_2 respectively. $\tilde{\lambda}^{(1)}, \tilde{\lambda}^{(2)}$ are the trending structure state space vector of l_1, l_2 . Hamming distance between $\tilde{\lambda}^{(2)}$ and $\tilde{\lambda}^{(2)}$ is defined as follows,

$$H(\tilde{\lambda}^{(1)}\tilde{\lambda}^{(2)} = \sum_{i=1}^{n-k+1} h_i$$

$$h_i = \begin{cases} 1, & p_i \neq p_2, \lambda_{1i}\lambda_{2i} > 0\\ 0, & \tilde{\lambda}^{(1)} = \tilde{\lambda}^{(2)} \\ 2, & p_i \neq p_2, \lambda_{1i}\lambda_{2i} < 0. \end{cases}$$
(12)

in which, $l_1 = (\lambda_{11}, ..., \lambda_{1k}), l_2 = (\lambda_{21}, ..., \lambda_{2k})$

Property 2 $\cdot 0 \le H(\tilde{\lambda}^{(1)}, \tilde{\lambda}^{(2)}) \le 2k$

If $H(\tilde{\lambda}^{(1)}, \tilde{\lambda}^{(2)}) = 0$, then K-time sub sequence s_1 has the same trending variation ratio with s_2 .

The smaller $H(\tilde{\lambda}^{(1)}, \tilde{\lambda}^{(2)})$ is, the better pattern matching is.

Here, we give a pattern difference measurement method, we can easily get the same or similar pattern with goal pattern (predictable sub time sequence). In a intuitionistic sense, $H(\tilde{\lambda}^{(1)}, \tilde{\lambda}^{(2)})$ reflects the synthetical similarity between l_1 and l_2 i = 1, 2..., n-k. So, obtaining the relationship and extracting useful rules among these patterns is a problem.

The pattern matching model is devised as follows,

$$Min \ H(s_q, \hat{\lambda}^{(i)})$$

s.t. $\lambda_{si} \lambda_{ii} > 0$

i = 1, 2, ..., n - k

4.3.3 EXTRACTING PREDICTABLE RULES

In fact, each object in Table3 denotes a known predictable rule. These predictable rules are wrote like this according to Definition 10.

$$eg.if \ descend_{rapid} \rightarrow ascend_{moderate}$$

$$\rightarrow ascend_{rapid} \rightarrow ascend_{slow} \rightarrow ascend_{moderate}$$
the decend_{slow}

In the trending variation ratio structure predictable information system (See table 3), q is our prediction aim, s_q is predictable pattern, we can

predict the q by conditional expression C={ λ_{n-k+1} , λ_{n-k+2} ,..., λ_{n-1} } in s_q.

Definition 14 Let Sim(x, y) be the function of the similarity about x and y. For prediction sequence s_q and l_i , its similarity is defined as follows

$$Sim(s_q, l_i) = \frac{1}{H(s_q, l_i)}$$
(13)

in which q=-1,0,1;i=1,2,...,n-k.

Note 1 The smaller $H(s_q, l_i)$ is, the better $Sim(s_q, l_i)$ is, i.e, the trusty q is.

Remark: The feature of the algorithm of trending variation ratio structure sequence based on rough set is concluded as follows,

Consider the conditional attribute sets belong to in-discernibility equivalence relation on objects, but not other objects. Hence, calculated capacity is lesser.

Description of trend structure classification is subtle.

Fuzzy discrete method accords with human intuitivism.

4.4 ALGORITHMS

A: Algorithm of Data Conversion and Resolution on $S(\lambda, k)$

Step1: Input $X = \{x_1, x_2, ..., x_n\}$ Computing Step2: **TVRSS** $\lambda = \left(\frac{\Delta_X^1}{\Delta_T^1}, \frac{\Delta_X^2}{\Delta_T^2}, \dots, \frac{\Delta_X^{n-1}}{\Delta_T^{n-1}}\right) = (\lambda_1, \lambda_2, \dots, \lambda_{n-1}) \operatorname{accordi}$ ng to $\lambda_i = \frac{\Delta_X^i}{\Delta_T^i}$. Step3: $S(\lambda, k) \leftarrow \phi$ For (t=1; t<n-k; t++) { $U(t) = (\lambda_1, \lambda_2, \dots, \lambda_{t+k-1});$ $S(T_r,k) \leftarrow S(T_r,k) \cup \{U(t)\}$ Step4: output $S(\lambda, k)$ **B**: Adjacence Algorithm of Computing $S(\lambda, k-1)$ and l_{n-1} Step1: Input $S(\lambda, k-1)$ $M \leftarrow 0$ Step2. For $(i = 1; i < |S(\lambda, k-1)|; i++)$ $\widetilde{\lambda} \leftarrow F(\lambda)$ For $\lambda^{n-k} \in \widetilde{\lambda}$, calculating $H(s_a, \lambda^{n-k})$ $Min(H(s_q,\lambda^{n-k}))$

}

5. EXPERIMENT

As we all known, stock data is a typical time

series database. Stock code, opening price and closing price for every day are kept in the stock database. Here, stock code is static attribute, but opening price and closing price are dynamic attributes which change with time. Investor pay more attention to the alteration of opening price and closing price. In this paper, closing price is considered and analyzed.

We make short-term closing price forecast of Shen zhen Developing Bank (China) stock data according to the 32 transaction data (from March 1, 2005 to April 13, 2005, see Table4) [10].

5.1 EXPERIMENT STEP

Step 1: After computing trending variation ratio structure sequence, we can compute the trending variation ratio structure sequence of stock time series according to definition 2. (see table 4)

The stock series is expressed as follows according to definition 1:

X={6.48, 6.40, 6.38, 6.44, 6.33, 6.38, 6.36, 6.28, 6.10, 6.12, 6.10, 5.99, 5.94, 6.0, 5.93, 5.99, 5.54, 5.37, 5.40, 5.38, 5.30, 5.30, 5.09, 5.20, 5.52, 5.42, 5.5, 5.7, 6.29, 6.8, 6.88, 6.7}

 Table 4. Transaction data (t, p denote time and closing price respectively)

t	1	2	3	4	5	6	7	8
р	6.48	6.40	6.38	6.44	6.33	6.38	6.36	6.28
t	9	10	11	12	13	14	15	16
р	6.10	6.12	6.10	5.99	5.94	6.0	5.93	5.99
t	17	18	19	20	21	22	23	24
р	5.54	5.37	5.40	5.38	5.30	5.30	5.09	5.20
t	25	26	27	28	29	30	31	32
Р	5.52	5.42	5.5	5.7	6.29	6.8	6.88	6.7

Trending variation ratio structure sequence of stock time series is,

 $\lambda = \{-0.02, 0.06, -0.08, -0.04, -0.11, -0.06, -0.13, -0.04, -0.0133, -0.09, -0.06, 0.04, -0.04, 0.0033, -0.4, -0.18, 0.04, 0, -0.0333, -0.2, 0.11, 0.39, -0.06, 0.07, 0.12, 0.56, 0.62, 0.0967, -0.44, 0.24\}$

Step 2: Let mobile windows size k=5, k-time sub series are obtained according to definition 3. (see Table 5)

Step 3: Convert TVRSS into predictable decision-making information system according to table 3 (see Table 5). Here, q is our prediction aim.

Step 4: Fuzzy discrete trending variation ratio according to Data pretreatment method in section.4.3.1. (see table 6)

Step 5: Computing the Hamming distance between s_q and l, i.e, $H(s_q, l)$. Due to definition 13, $H(s_q, l)$ are solved as follows (see Table 7).

Step 6: Computing the maximal similarity degree of Hamming distance according to Eq. (13).

If

$$H(s_q, s_{25}) = \frac{1}{3}$$

 Table 6. Trending prediction table of stock time series

Finally, we learnt similarity degree of Hamming distance according is maximal when $s = s_{25}$. So, the similarity is the best among all feature sub sequences. Hence, the rules of sequence s_{25} is inserted in knowledge database, helping make future prediction.

Because of above analysis, we can get the experimental result that the closing price at time 33 is higher than its former closing price. In fact, observing closing price at time 33 is higher than its former closing price. From the decision-making rule point of view, we can gain such rule as follow,

Decision-making rule $A_1 = ascend_{moderate}, A_2 = ascend_{apid}, A_3$

$$= descend_{mod\,erate}, A_4 = ascend_{mod\,erate}, then$$

 $D = ascend_{moderate}$. i.e, If closing price of the stock market keeps rising for five days and declines next day, then the closing price will be higher than former closing price in the future.

 Table 5. Trending prediction table of stock time series

	A_1	A_2	A ₃	A_4	D
s ₁	-0.02	0.06	-0.08	-0.04	0.11
s ₂	0.06	-0.08	-0.04	0.11	-0.06
S ₃	-0.08	-0.04	0.11	-0.06	-0.13
s_4	-0.04	0.11	-0.06	-0.13	-0.04
s_5	0.11	-0.06	-0.13	-0.04	-0.0133
s ₆	-0.06	-0.13	-0.04	-0.0133	-0.09
\mathbf{S}_7	-0.13	-0.04	-0.0133	-0.09	-0.06
s ₈	-0.04	-0.0133	-0.09	-0.06	0.04
S 9	-0.0133	-0.09	-0.06	0.04	-0.04
s_{10}	-0.09	-0.06	0.04	-0.04	0.0033
s_{11}	-0.06	0.04	-0.04	0.0033	-0.4
s ₁₂	0.04	-0.04	0.0033	-0.4	-0.18
s ₁₃	-0.04	0.0033	-0.4	-0.18	0.04
s ₁₄	0.0033	-0.4	-0.18	0.04	0
s ₁₅	-0.4	-0.18	0.04	0	-0.0333
s ₁₆	-0.18	0.04	0	-0.0333	0
s ₁₇	0.04	0	-0.0033	0	-0.2
s ₁₈	0	-0.0033	0	-0.2	0.11
S ₁₉	-0.0033	0	-0.2	0.11	0.39
s ₂₀	0	-0.2	0.11	0.39	-0.06
s ₂₁	-0.2	0.11	0.39	-0.06	0.07
s ₂₂	0.11	0.39	-0.06	0.07	0.12
s ₂₃	0.39	-0.06	0.07	0.12	0.56
s ₂₄	-0.06	0.07	0.12	0.56	0.62
s ₂₅	0.07	0.12	0.56	0.62	0.0967
s ₂₆	0.12	0.56	0.62	0.0967	-0.44
S ₂₇	0.56	0.62	0.0967	-0.44	0.24
Sq	0.62	0.0967	-0.44	0.24	goal

	A_1	A_2	A ₃	A_4	D
S ₁	0000001	0010000	0000010	00000	
S ₂	0010000	0000010	0000001	01000	00 0000010
S3	0000010	0000001	0100000	00000	10 0000010
S4	0000001	0100000	0000010	00000	
S ₅	0100000	0000010	0000010	00000	0000001
s ₆	0000010	0000010	0000001	00000	
S7	0000010	0000001	0000001	00000	
S ₈	0000001	0000001	0000010	00000	10 0010000
S9	0000001	0000010	0000010	00100	
S ₁₀	0000010	0000010	0010000	00000	
s ₁₁	0000010	0010000	0000001	00100	
s ₁₂	0010000	0000001	0010000	00001	
s ₁₃	0000001	0010000	0000100	00001	
s ₁₄	0010000	0000100	0000100	00100	
S ₁₅	0000100	0000100	0010000	00001	
S ₁₆	0000100	0010000	0000100	00000	
S ₁₇	0010000	0000100	0000001	00010	
S ₁₈	0000100	0000001	0001000	00001	
S ₁₉	0000001	0001000	0000100	01000	
S ₂₀	0001000	0000100	0100000	10000	
S ₂₁	0000100	0100000	1000000	00000	
S ₂₂	0100000	1000000	0000010	01000	
S ₂₃	1000000	0000010	0100000	01000	
s ₂₄	0000010	0100000	0100000	10000	
S ₂₅	0100000	0100000	1000000	10000	
S ₂₆	0100000	1000000	1000000	01000	
S ₂₀ S ₂₇	1000000	1000000	0100000	00001	
S _q	1000000	0100000	0000100	10000	
Υq	11				50 5000
		adle 7.	H(sq, si) tab	ne	
s	$H(s_{q},s_{i})$	s	$H(s_q, s_i)$	s	$H(s_q, s_i)$

s	$H(s_q, s_i)$	s	$H(s_q, s_i)$	s	$H(s_q, s_i)$
s1	2+1+1+2=6	s_2	1+2+1+1=5	\mathbf{S}_3	2+2+2+2=8
s4	2+0+1+2=5	s_5	1+2+1+2=6	s_6	2+2+1+2=7
s7	2+2+1+2=7	S_8	2+2+1+2=7	S 9	2+2+1+1=6
s10	2+2+2+2=8	\mathbf{s}_{11}	2+1+1+1=5	\mathbf{s}_{12}	1+2+2+2=7
s13	2+1+0+2=5	s_{14}	1+2+0+1=4	\mathbf{s}_{15}	2+2+2+2=8
s16	2+1+2+2=7	\mathbf{s}_{17}	1+2+1+2=6	S ₁₈	2+2+2+2=8
s19	2+2+0+1=5	S ₂₀	2+2+2+0=6	s_{21}	2+0+2+2=6
s22	1+1+1+1=4	s ₂₃	0+2+2+1=5	s ₂₄	2+0+2+0=4
s25	1+0+2+0=3	s ₂₆	1+1+2+1=5	s ₂₇	0+1+2+2=5

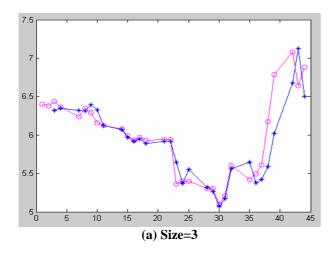
5.2 EXPERIMENT RESULT

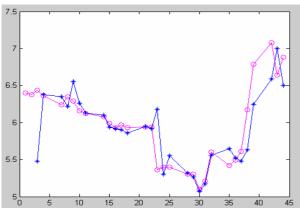
In this paper, we utilized different Mobile window size to calculating the prediction result and accuracy.

Factors	Hamming	Matching	Prediction	Confidence
Size	Distance	No	Results	
<i>k</i> = 3	0+1=1	2	Descend	50%
			moderate	
	0+1=1		Descend	50%
			slow	
<i>k</i> = 4	1+1+1=3	2	Ascend	50%
			moderate	
	1+1+1=3		Ascend	50%
			rapid	
<i>k</i> = 5	1+1+1+1	1	Ascend	100%
	=4		moderate	
<i>k</i> = 6	#	0	#	
<i>k</i> = 7	#	0	#	

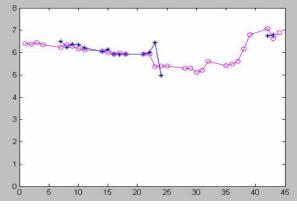
Table 8. Pattern results for different mobile window sizes

So, we can easily get the optimal mobile window size=3, and the prediction results (see Fig2.(a)).





(b) Size=4



(c) Size=5

Fig. 2 – Actual curve and prediction curve for different mobile window sizes

6. CONCLUSION

This paper mainly discussed the time-series data prediction based on trending variation ratio structure sequence and rough set. To obtain various k-time series, mobile window method is adopted. As a matter of fact, each sub time series is pattern. Trending variation ratio structure sequence is applied to sub time series in order to get important attribute which depict each sub time series. To predict unknown data or information in the future, trending variation ratio structure predictable information system is constructed. Hamming distance is adopted in pattern identification. Our method is applied to stock market data prediction.

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